

# ParaDime

A FRAMEWORK FOR PARAMETRIC  
DIMENSIONALITY REDUCTION



Andreas Hinterreiter, Christina Humer, Bernhard Kainz, Marc Streit  
EuroVis 2023



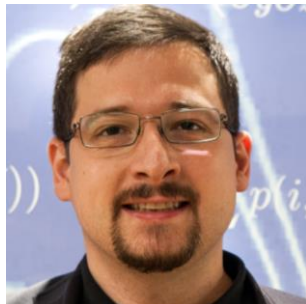
Imperial College  
London



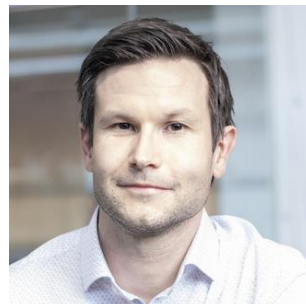
Andreas  
Hinterreiter



Christina  
Humer



Bernhard  
Kainz



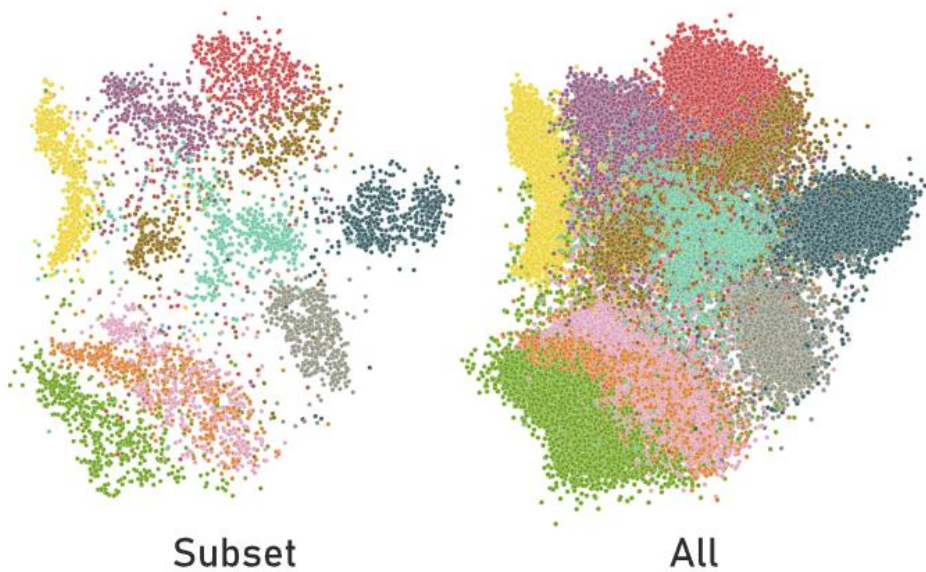
Marc  
Streit





Value of feature 8

A vertical color scale ranging from -4.5 (dark teal) at the bottom to 1.5 (yellow) at the top, with intermediate markers at -3.0 and 0.0.



- 0
- 1
- 2
- 3
- 4
- 5
- 6
- 7
- 8
- 9

```

relations:
  - name: dists hd
    level: global
    type: pairwise
    options:
      metric: euclidean
  - name: dists ld
    level: batch
    type: pairwise
    options:
      metric: euclidean

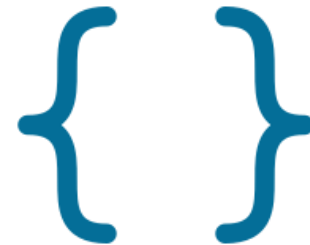
losses:
  - name: mds
    type: relation
    func: mse
    keys:
      rels:
        - dists hd
        - dists ld
    training phases:
      - loss:
          components: mds
  
```



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Parameterize



Share & Reuse



Customize



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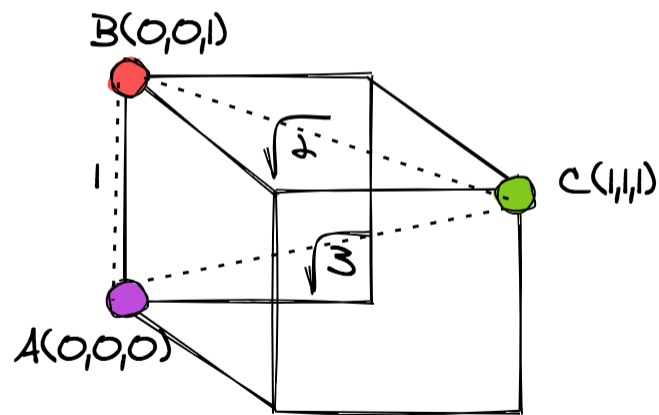


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# SIMILARITIES BETWEEN METHODS



- MDS
- Isomap
- t-SNE
- LargeVis
- UMAP

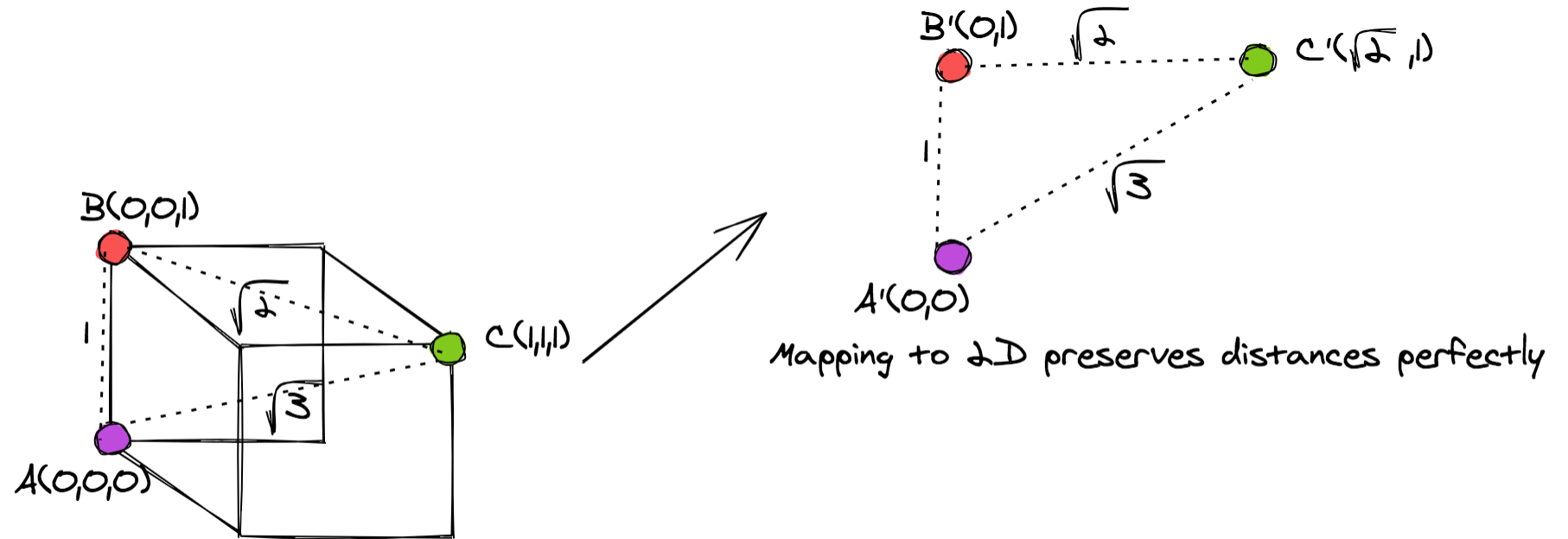


<https://stackabuse.com/guide-to-multidimensional-scaling-in-python-with-scikit-learn/>

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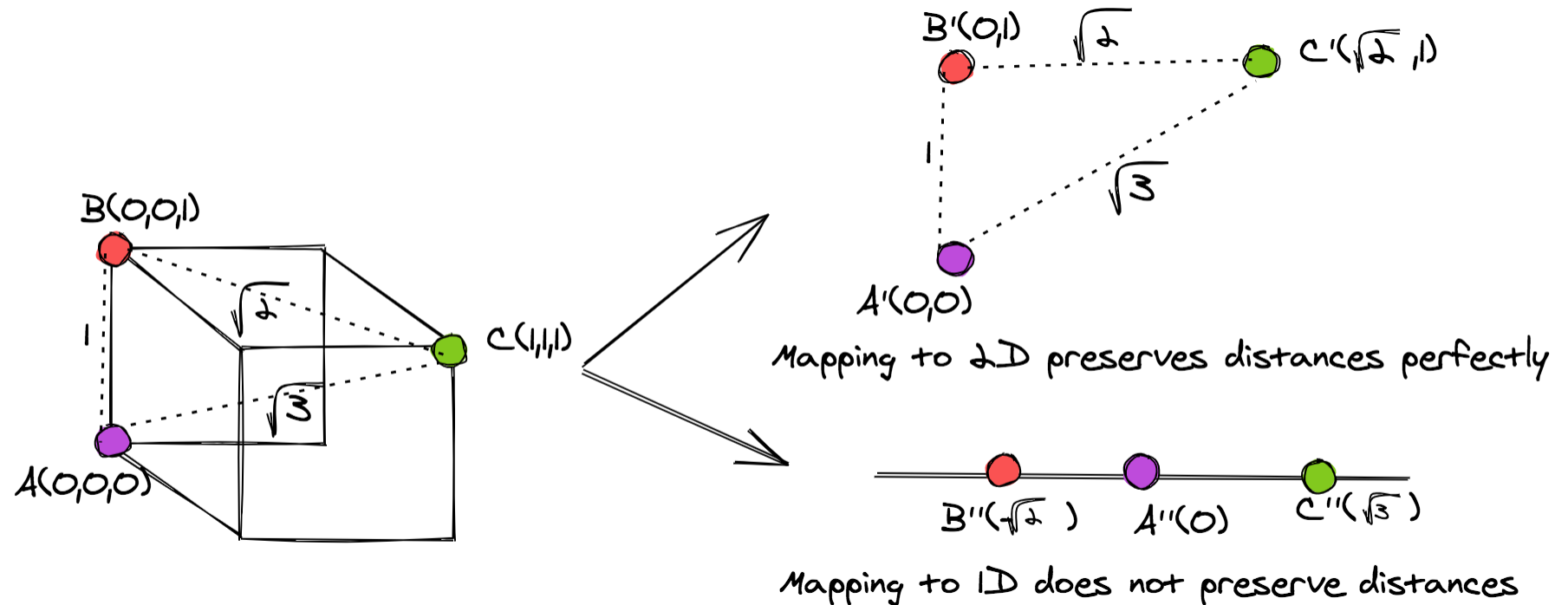


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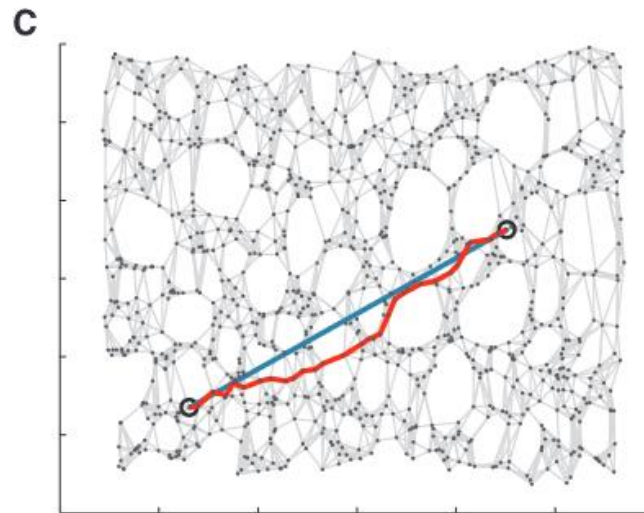
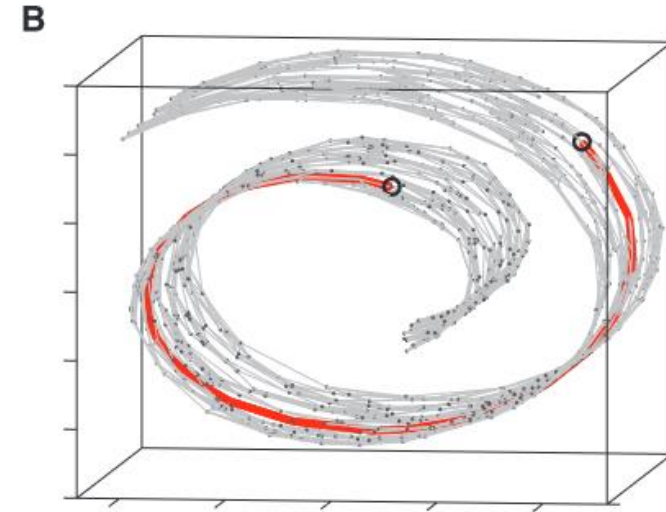
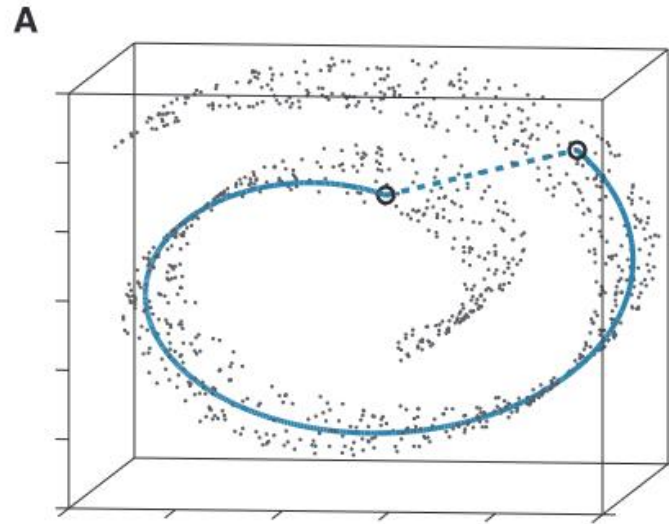
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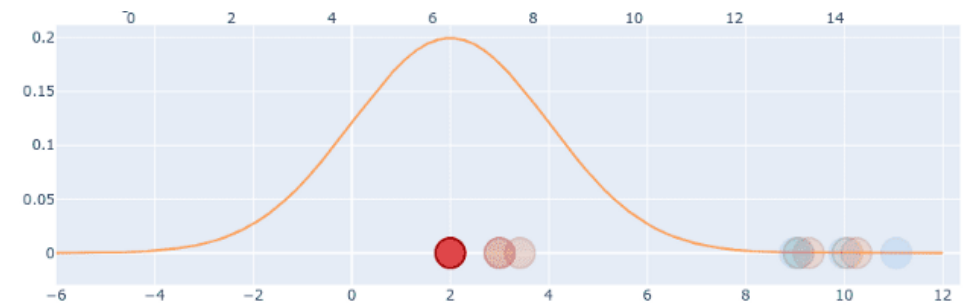
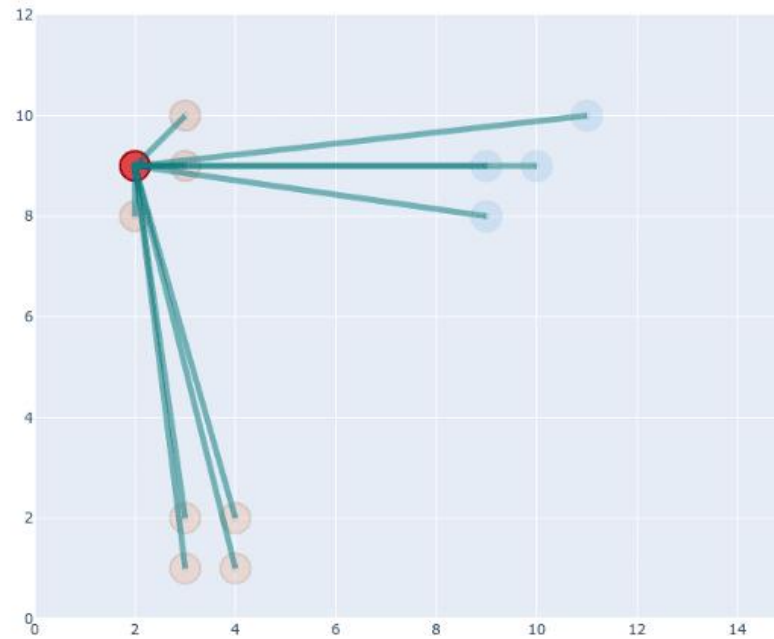


Tenenbaum, J. B. (2000). A Global Geometric Framework for Nonlinear Dimensionality Reduction. *Science*, 290(5500), 2319–2323.

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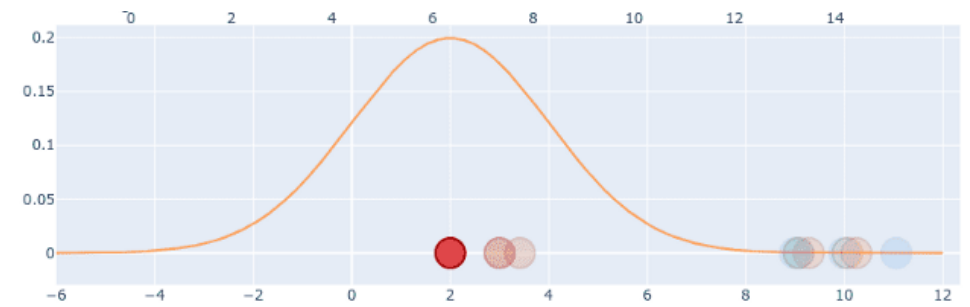
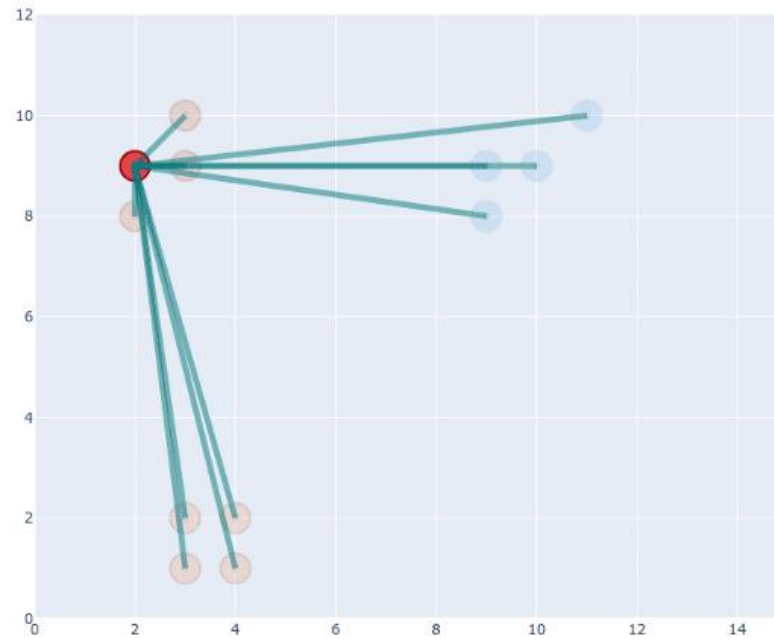


<https://towardsdatascience.com/t-sne-clearly-explained-d84c537f53a>

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- MDS
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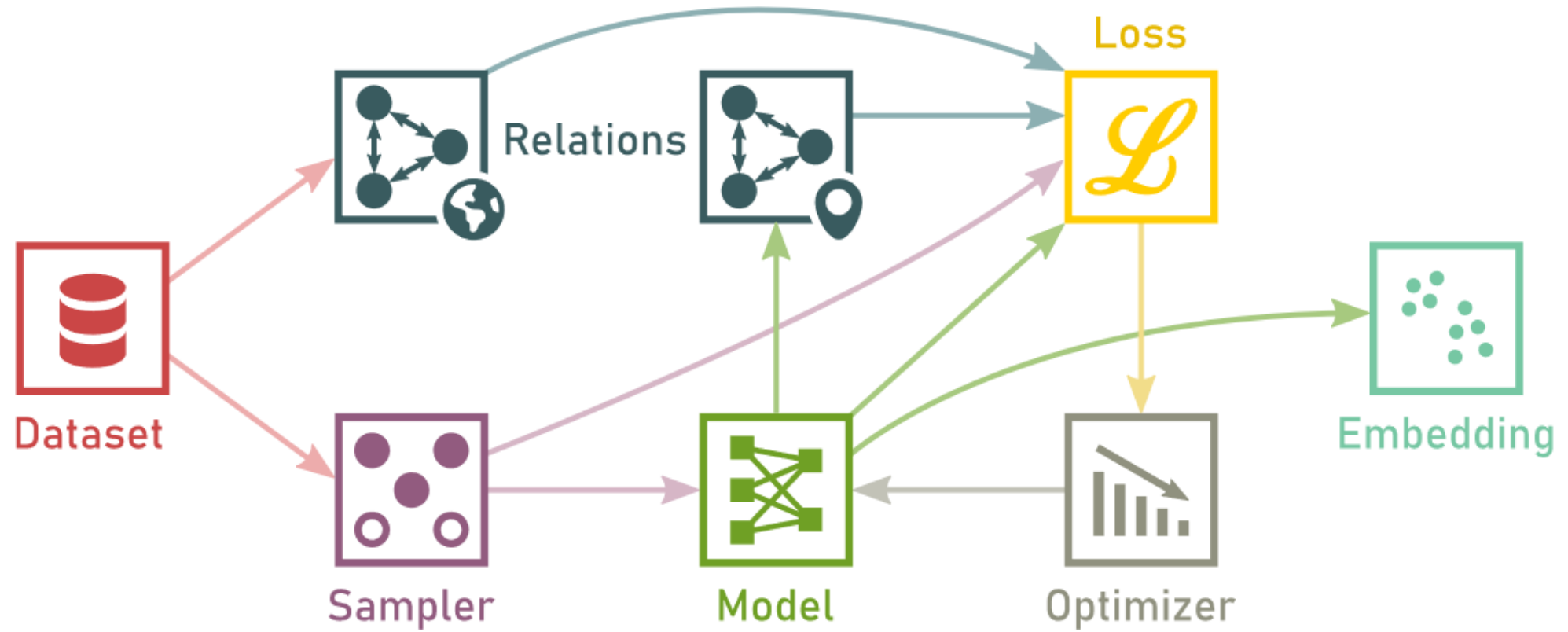


- MDS
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- t-SNE
- LargeVis
- UMAP

## Summary

1. Compute distances in high-dimensional space
2. Optionally transform HD distances
3. Arrange points in low-dimensional space and compute distances
4. Optionally transform LD distances
5. Make (transformed) distances match

# DATA FLOW





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- Non-parametric embeddings:

$$\text{DR}(\{x_1, \dots, x_n\}) = \arg \min_{y_i \in \mathbb{R}^k} \mathcal{L}(\{x_1, \dots, x_n\}, \{y_1, \dots, y_n\})$$

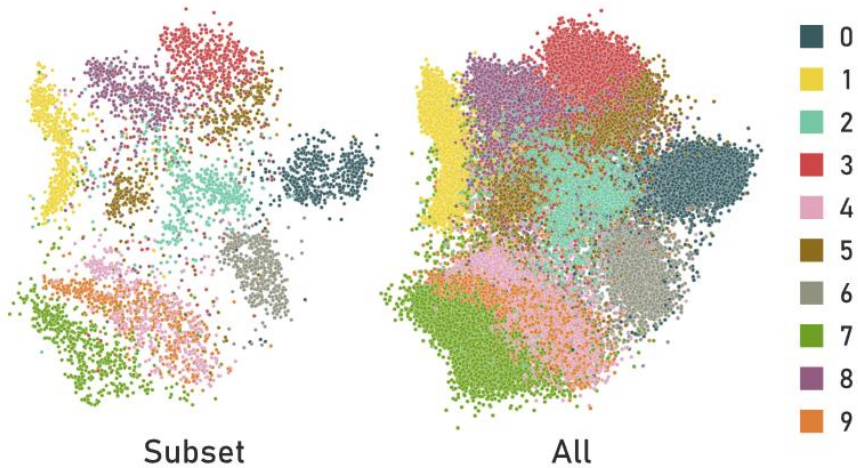
- **Parametric** embeddings:

$$\text{DR}_{\text{param}}(\{x_1, \dots, x_n\}) = \arg \min_{f \in F} \mathcal{L}(\{x_1, \dots, x_n\}, \{f(x_1), \dots, f(x_n)\})$$

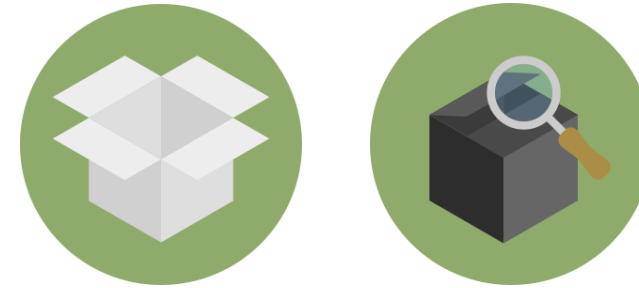
# PARAMETRIC EMBEDDINGS



- Out-of-sample extension



- Potentially explainable



- Modern infrastructure

- Differentiable

$$\frac{\partial f}{\partial x}$$

- Customizable

$$\mathcal{L} = \sum_{i=1}^n w_i \times \mathcal{L}_i$$



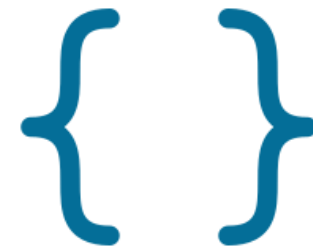




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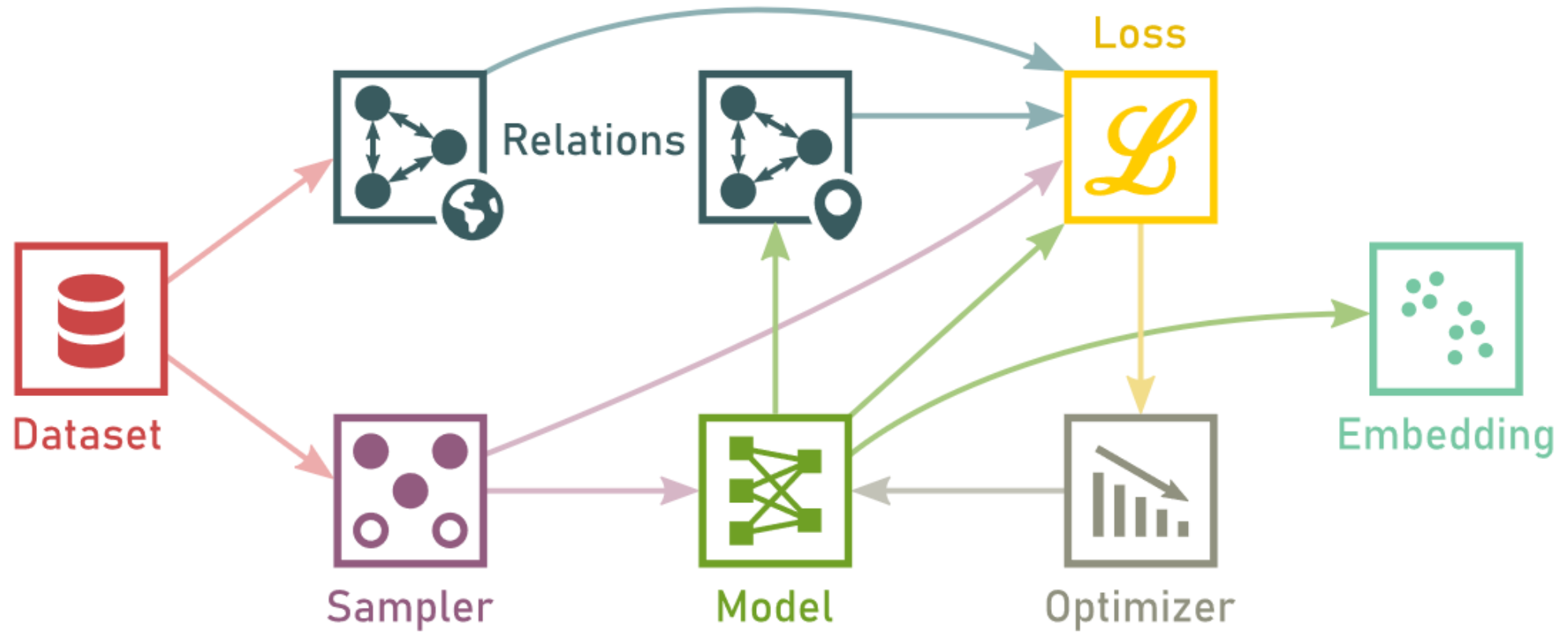


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# DATA FLOW



`relations:`

`losses:`

`training phases:`

## relations:

- name: dists hd  
level: global  
type: pairwise  
options:
  - metric: euclidean
- name: dists ld  
level: batch  
type: pairwise  
options:
  - metric: euclidean

## losses:

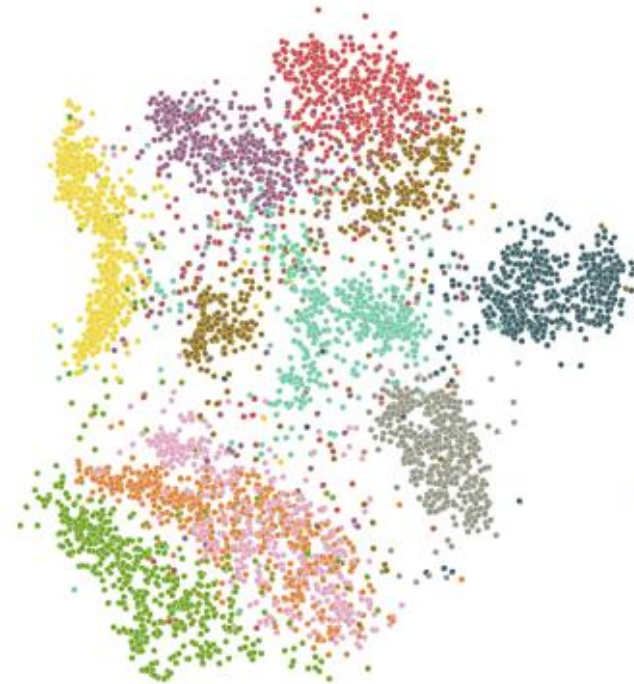
- name: mds  
type: relation  
func: mse  
keys:
    - rels:
      - dists hd
      - dists ld
- training phases:
- loss:
    - components: mds

# GRAMMAR & SPECIFICATIONS

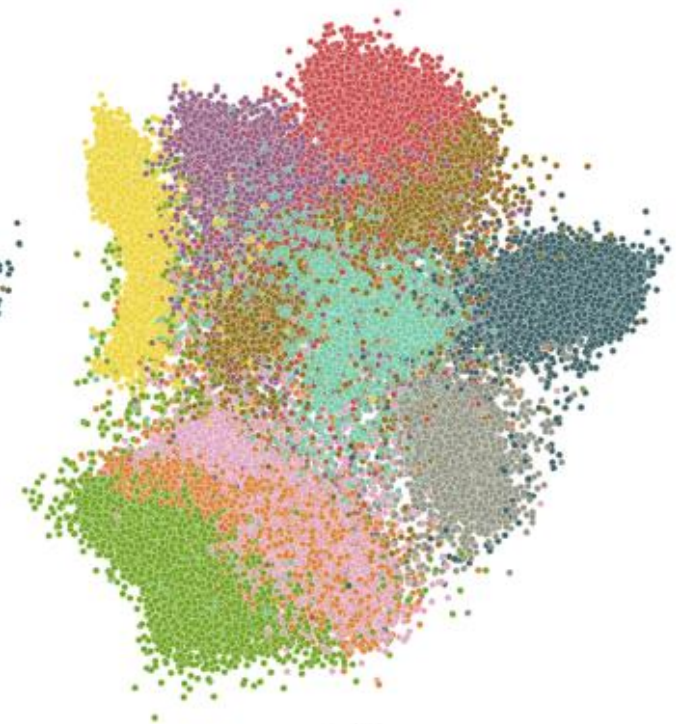


```
derived data:  
- name: pca  
  data func: pca  
  keys: [[data, main]]  
relations:  
- name: p  
  level: global  
  type: neighbor  
  data: main  
  options:  
    metric: euclidean  
  transforms:  
    - type: perplexity  
      options:  
        perplexity: <p>  
    - type: symmetrize  
    - type: normalize  
- name: q  
  level: batch  
  type: pairwise  
  data: main  
  options:  
    metric: euclidean  
  transforms:  
    - type: t-dist
```

```
options:  
  alpha: 1.  
  - type: normalize  
losses:  
- name: init  
  type: position  
  func: mse  
  keys:  
    data: [main, pca]  
- name: emb  
  type: relation  
  func: kl div  
  keys:  
    rels: [p, q]  
training phases:  
# pca initialization  
- loss:  
  components: [init]  
  sampling:  
    type: item  
# main embedding  
- loss:  
  components: [emb]  
  sampling:  
    type: item
```



Subset



All





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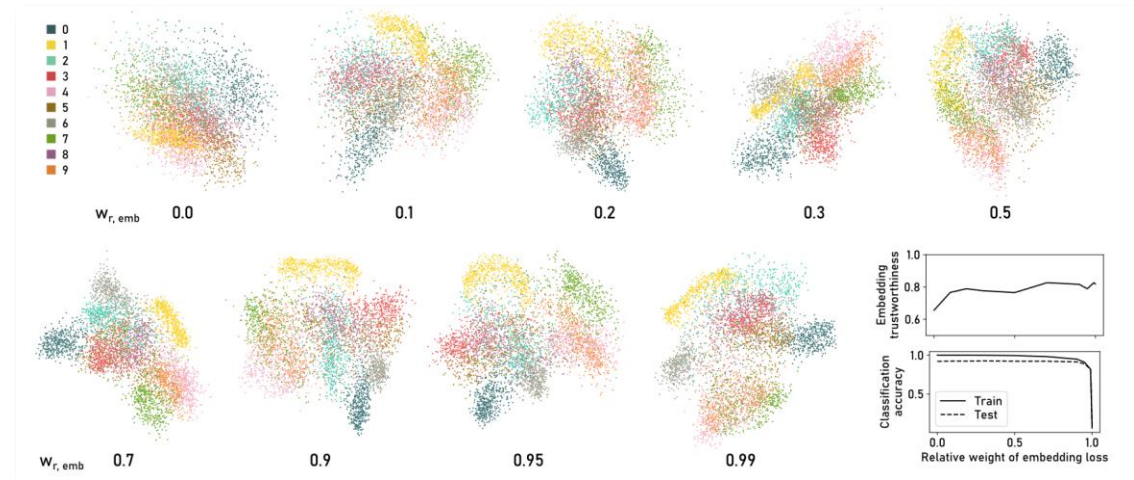
# CUSTOMIZATION EXAMPLES



## ■ Hybrid/multitask routines

- Classification
- Reconstruction

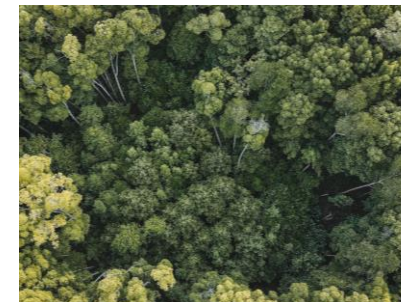
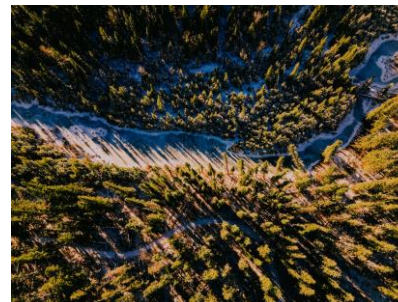
```
relations: <UMAP relation specs>  
losses: [<UMAP loss>, <classification loss>]  
training phases:  
- loss:  
  components: [umap, class]  
  weights: <w>
```



## ■ Multi-phase routines

## ■ Supervised routines

## Forest covertype Dataset

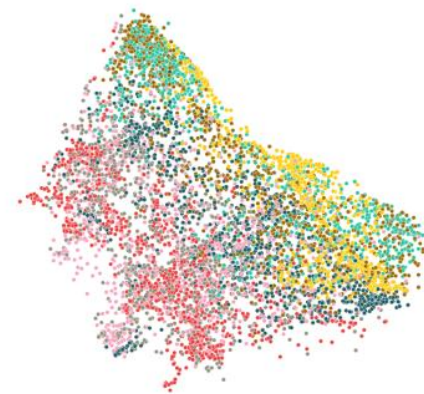


# SUPERVISED DR - TRIPLETS



- Aspen
- Cottonwood/willow
- Douglas-fir
- Krummholz
- Lodgepole pine
- Ponderosa pine
- Spruce/fir

$R = w(\text{t-SNE}) / w(\text{Triplet})$



Parametric t-SNE (ParaDime)



t-SNE (scikit-learn)



# SUPERVISED DR - TRIPLETS

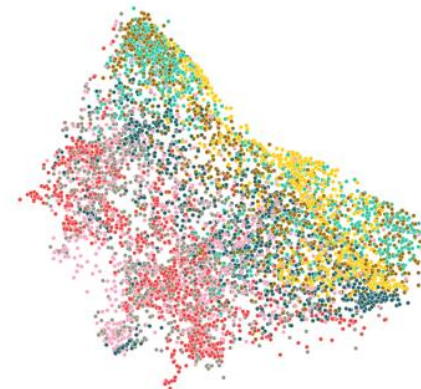


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$R = w(\text{t-SNE}) / w(\text{Triplet})$



R = 10



Parametric t-SNE (ParaDime)



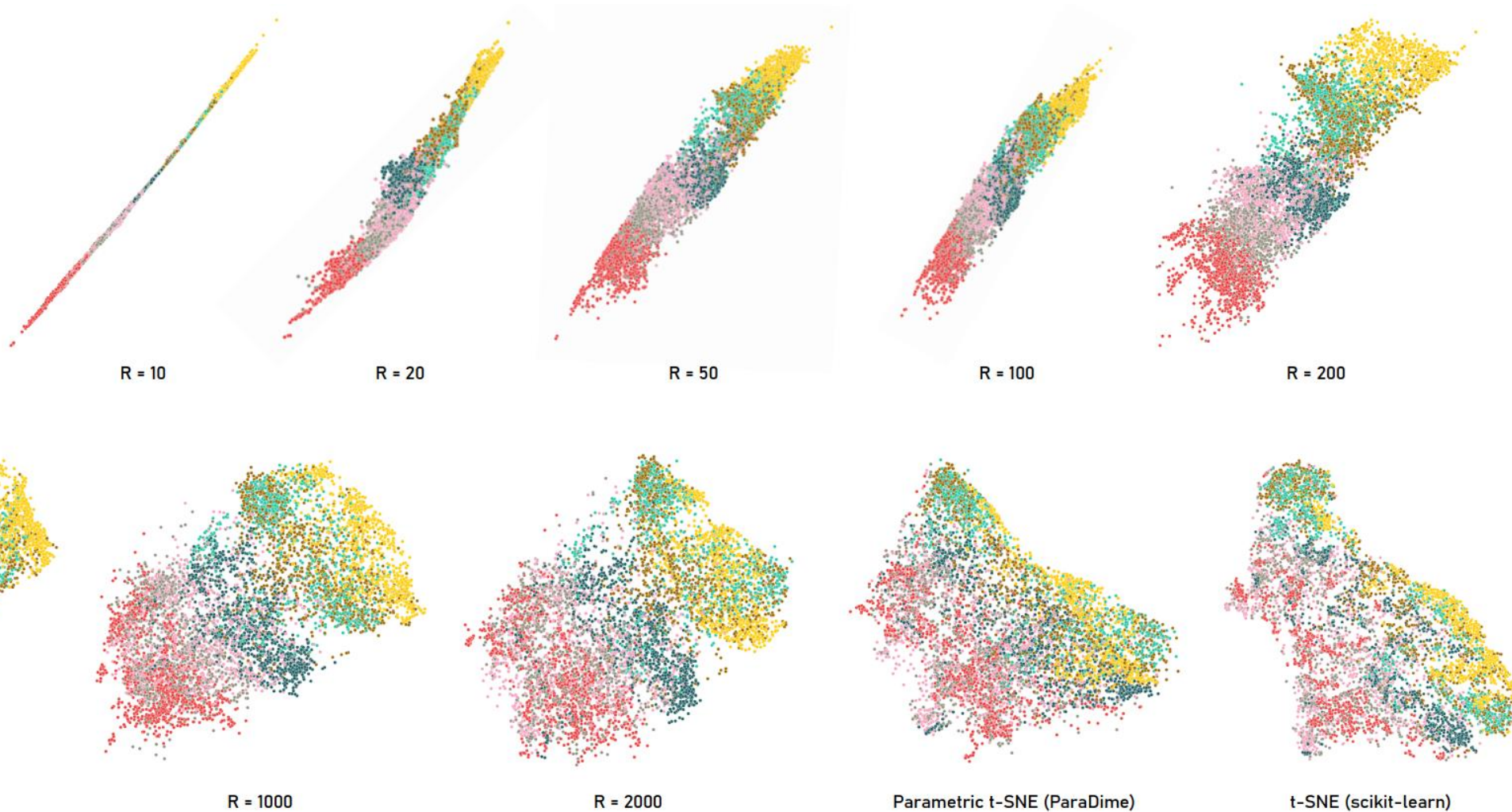
t-SNE (scikit-learn)

# SUPERVISED DR - TRIPLETS

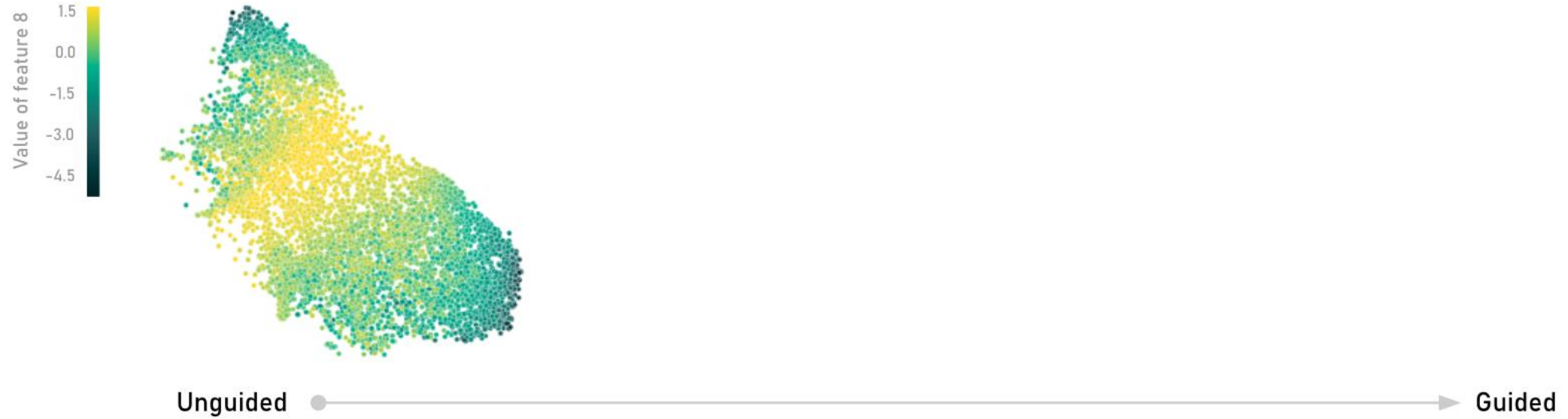


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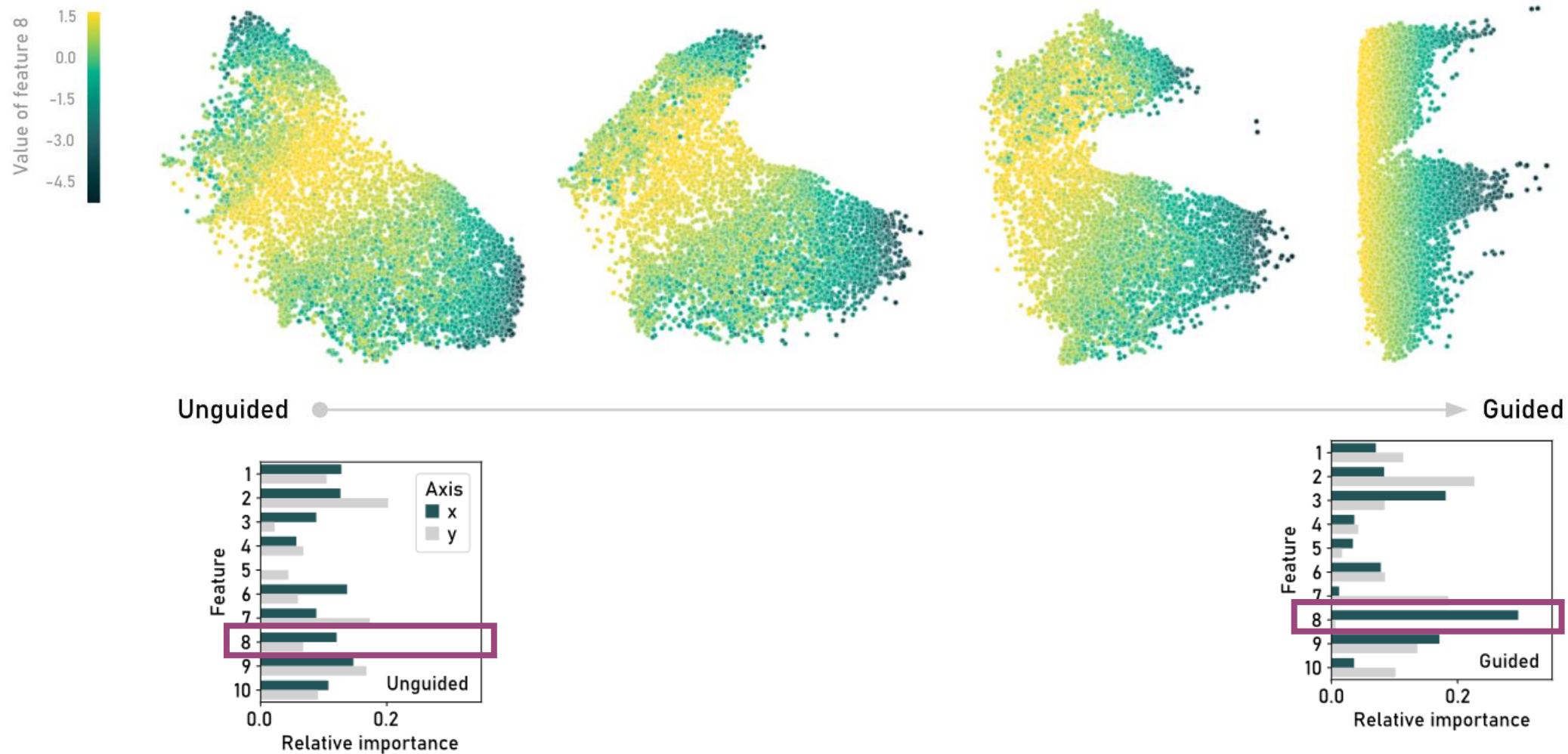
# SUPERVISED DR – CORRELATION



# SUPERVISED DR – CORRELATION



# SUPERVISED DR – CORRELATION





**Read the Docs**



Unify



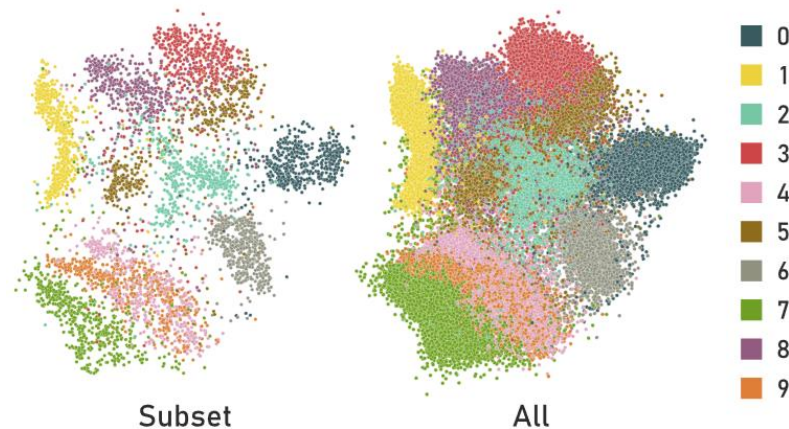
Parameterize



Customize



Share



**JKU**

**JOHANNES KEPLER  
UNIVERSITÄT LINZ**